

# 'LAWS OF MOTION'

## FORCE

Any type of push or pull which is tried to change the state of rest or, uniform motion.

NOTE → Resultant force on body may change.

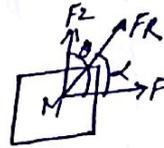
- \* Its shape
- \* Its direction
- \* both
- \* shape of body.

\* Force is a vector quantity that's why vector addition of individual forces.

$$\vec{F}_R = \vec{F}_1 + \vec{F}_2 + \dots + \vec{F}_n$$

$$\# N=2 \Rightarrow \vec{F}_R = \vec{F}_1 + \vec{F}_2$$

$$|\vec{F}_R| = \sqrt{F_1^2 + F_2^2 + 2F_1F_2\cos\theta}$$
$$\downarrow \text{and } \alpha = \frac{F_2\sin\theta}{F_1 + F_2\cos\theta}$$



$$\# F_1 = F_2 = F$$

$$F_R = 2F\cos(\theta/2)$$
$$\alpha = \theta/2$$

## INERTIA

Property which is maintain the state of rest or state of uniform motion.

NOTE → \* Inertia is directly proportional to the mass.

- \* It only depend on mass. It is independent from shape & state of body.
- \* Same mass object in different shape represent same inertia.
- \* If two same mass object one object in rest & another move with uniformly or, in uniform motion represent same inertia.

## NEWTON'S 1ST LAW

External force is Required to change the state or, state of uniform motion.

Newton 1st law explain inertia of body that's why called law of inertia.

### Types of Inertia

1a) → Inertia of Rest → body can't change its state of rest by its self.  
EX → \* If bus suddenly move forward than passenger in bus moving backward.  
\* Sudden jerk is applied on blanket dust particle removed from it.

1b) → Inertia of Motion → body can't change its state of motion by itself.  
EX → \* If bus suddenly stop than passenger moving forward.  
\* Fast baller transfer its velocity to the ball.

1c) → Inertia of Direction → Body can't change its direction by its self.  
EX → \* If bus turns right than passenger in bus moving left or, outward to the centre of circular path than force which is act in outward direction is called centrifugal force.

\* Mud particle attached with wheel moving tangential when it is detach from wheel.

NOTE → Newton's 1st law & Introduce force but its measurement or Magnitude explain from Newton's 2nd law.

NETONN'S 2nd LAW

External force applied on body is  $\propto$  to Rate of change in momentum w.r.t time.

$$\vec{F}_{ex} \propto \frac{d\vec{p}}{dt}$$

$$\vec{F}_{ex} = k \frac{d\vec{p}}{dt} \quad (k=1)$$

$$\vec{F}_{ex} = \frac{d\vec{p}}{dt}$$

# Momentum ( $\vec{p}$ )

$$\vec{p} = m\vec{v}$$

$$\vec{F}_{ex} = \frac{d\vec{p}}{dt} = \frac{d(m\vec{v})}{dt}$$

$\vec{p} \Rightarrow$  direction of momentum in the direction of velo.

# change in momentum ( $\Delta\vec{p}$ )

$$d\vec{p} = \vec{F}_{ex} dt$$

$$\vec{F}_{ex} = \frac{d\vec{p}}{dt} = \frac{d}{dt}(m\vec{v})$$

↓ direction of change in momentum in the direction ext force.

\*\* |a| → v = c  
m → change

$$\vec{F}_{ex} = v \frac{dm}{dt}$$

\* |b| → m = const.  
v → change

$$\vec{F}_{ex} = m \frac{dv}{dt} = m\vec{a}$$

\* |c| → m → change  
v → change.

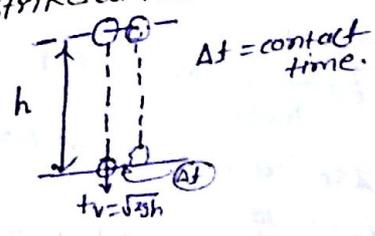
$$\vec{F}_{ex} = ma + v \frac{dm}{dt}$$

\*  $\frac{dv}{dt} \Rightarrow$  Rate of change in velo = a

\*  $\frac{dm}{dt} \Rightarrow$  " " " " mass.

Application of newton's 2nd law

|1| → Particle is drop from height it strike at bottom & Rebound up to same height. [Elastic]



Ext. force is applied on ball.

$$\vec{F}_{ex} = \frac{m[-v-v]}{\Delta t} = \frac{-2mv}{\Delta t}$$

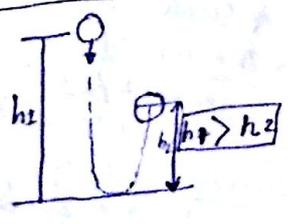
$$= \frac{-2m\sqrt{2gh}}{\Delta t}$$

|2| → Ball is drop height & perform Inelastic collision from bottom

$$\sqrt{v_1} = \sqrt{2gh_1}$$

$$\sqrt{v_2} = \sqrt{2gh_2}$$

$$|\vec{F}_{ex}| = \frac{m}{\Delta t} (\sqrt{2gh_1} + \sqrt{2gh_2})$$



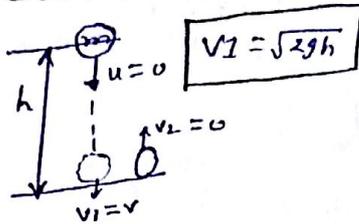
13] → Particle is drop from height it strike at bottom & perform perfectly elastic collision with bottom surface.

Force on ball

$$\vec{F}_{ex} = \frac{d\vec{p}}{dt} = \frac{0 - mv}{t} = -\frac{m\sqrt{2gh}}{t}$$

$$\vec{F}_{ex} = \frac{mv}{t} = \frac{m}{t}\sqrt{2gh}$$

Force on surface



14] → 'N' particle strike ~~strike~~ per second vertical surface at angle 'θ' from its normal with speed 'v'

1a] → Surface is Reflecting (Perfectly)

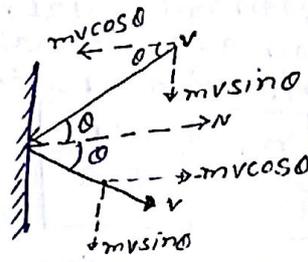
$$\vec{F}_{ext} = \frac{d\vec{p}}{dt}$$

$$\vec{F}_{||} = \frac{d\vec{p}_{||}}{dt} = \frac{mv\sin\theta - mv\sin\theta}{t} = 0$$

$$\vec{F}_{\perp} = \frac{d\vec{p}_{\perp}}{dt} = \frac{(-mv\cos\theta) - (mv\cos\theta)}{t}$$

$$\vec{F}_{net} = \vec{F}_{\perp} = \left(-\frac{2mv\cos\theta}{t}\right)N$$

Force on particle.



Force on surface

$$\vec{F}_{ext} = \frac{N}{t}(2mv\cos\theta) = n(2mv\cos\theta)$$

$$n = \frac{N}{t} = \text{no. of particle incident per unit time}$$

1b] → surface is perfectly Absorbing

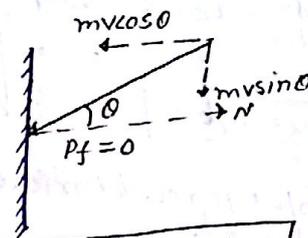
$$\vec{F}_{ex} = \frac{d\vec{p}}{dt}$$

$$\vec{F}_{||} = \frac{d\vec{p}_{||}}{dt} = \frac{0 - mv\sin\theta}{t} \neq 0$$

$$\vec{F}_{\perp} = \frac{d\vec{p}_{\perp}}{dt} = \frac{0 - (mv\cos\theta)}{t}$$

$$F_{\perp} = \left(-\frac{mv\cos\theta}{t}\right)N$$

$$F_{||} = \left(-\frac{mv\sin\theta}{t}\right)N$$



# Force on surface

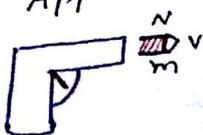
$$\vec{F}_{ex} = -\frac{N}{t}(mv) = -n(mv)$$

$$n = \frac{N}{t} = \text{no. of particle incident per unit time}$$

**NOTE** → \* Surface is partially Reflecting, partially absorbing then net force applied on surface in individual direction (⊥ or || to surface) is scalar addition of absorbing & reflecting part.

\* If particle is transmit than momentum transfer is zero.

15] → 'N' bullet of mass 'm' is fired from gun with speed 'v' then force Applied on gun.



\* Force on bullet

$$F_{ex} = \frac{dp}{dt} = \frac{mv - 0}{t} = \left(\frac{mv}{t}\right)N$$

\* Force on gun

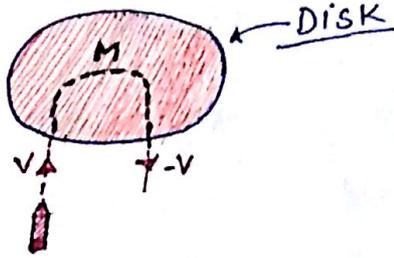
$$F_{ex} = -\left(\frac{mv}{t}\right)N$$

# Disc of mass 'm' is balanced in air when bullet strike normally with speed 'v' & reflect with same speed no. of bullet fired per unit time. (m → mass of bullet).

$$F_{\text{surface}} = \frac{N}{t} (2mv)$$

BHV

$$\frac{N}{t} = \frac{Mg}{2mv}$$



# Balloon of Hydrogen gas initially has mass 'm' & moves in a upward direction with acceleration 'a'. Some mass is added to the balloon & it will move downward with acceleration 'a' then calculate value of added mass.

$$m = \frac{2Ma}{g-a}$$

NOTE → upthrust of gases is independent from suspended mass. It only depend on type of gas & quantity of gas.

# H<sub>2</sub>-gas balloon of mass 'm' is moved in upward direction with constant acceleration 'a'. If some mass is removed from balloon. It will move with acceleration '2a' in upward direction. Then value of removed mass

$$m = \frac{Ma}{g+2a}$$

### Graphical meaning of Newton 2nd law

1) → slope of momentum time curve represent ext. force on particle.

$$F_{\text{ex}} = \frac{dp}{dt} = \frac{dy}{dx} = \text{slope}$$

$$F_{\text{ex}} = \text{slope} = 0$$

$$F_{\text{ex}} = \frac{dp}{dt} = \text{const.}$$

2) → Area enclosed b/w force & time curve represent change in momentum in a given interval.

$$\text{Area} = \int y dx$$

$$\text{Area} = \int_{t_1}^{t_2} F dt = d\vec{p} = \vec{p}_f - \vec{p}_i$$

# Impulse (I) → In a small time interval change in momentum on particle.

$$I = d\vec{p} = \int_{t_1}^{t_2} F \cdot dt$$

# particle of mass 'm' rotate in circular path of radius 'R' with uniform speed 'v' then Average force exerted on particle -

$$\Delta \vec{v} = 2v \sin(\theta/2)$$

$$\theta = \frac{R}{v} \omega = \omega t$$

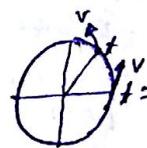
$$F_{\text{ex}} = \frac{mv^2}{R} = \frac{\sin(\theta/2)}{(\theta/2)}$$

(i) →  $\frac{1}{4}$  Rot or  $\pi/4$   

$$F_{\text{av}} = \frac{2\sqrt{2} mv^2}{\pi R}$$

(ii) →  $\frac{1}{2}$  Rot or  $\pi/2$   

$$F_{\text{av}} = \frac{2mv^2}{\pi R}$$

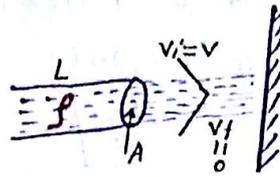


# Liquid of density ' $\rho$ ' flow from pipe of cross section area ' $A$ ' & length ' $L$ ' with uniform speed ' $v$ '. It strike at vertical surface & come in rest than force exerted on surface.

$$F_{ex} = \frac{dp}{dt} = \frac{0 - mv}{t}$$

$$|F_{ex}| = \frac{mv}{t} = \frac{(A\rho L)v}{t} \quad \left[ \frac{L}{t} = \text{velocity} \right]$$

$$* F_{ex} = A\rho v^2$$

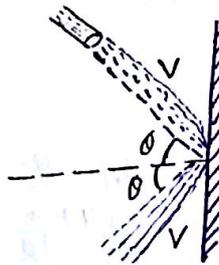


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#

$$F_{ex} = 2A\rho v^2 \cos\theta = FL$$

$$F_{II} = 0$$

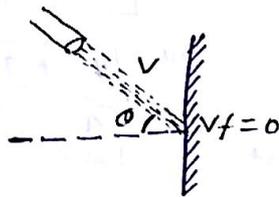


#

$$F_{II} = A\rho v^2 \sin\theta$$

$$F_L = A\rho v^2 \cos\theta$$

$$F_R = A\rho v^2 = \sqrt{F_{II}^2 + F_L^2}$$

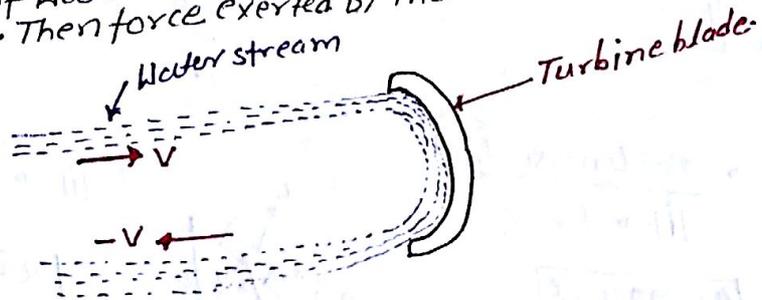


H.R

# A Stream of Water impinges on stationary dished turbine blade. The speed of water is ' $v$ ' both before & after strike the curved surface of the blade & the mass of water strike the blade per unit time is constant at value ' $\mu$ '. Then force exerted by the water on the blade.

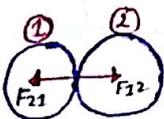
$$* F_{ex} = 2\mu v$$

mass of water strike the blade per unit time.



### Newton 3rd Law

Every Action produce equal and opposite Reaction.



$$\vec{F}_{12} = -\vec{F}_{21}$$

$$\vec{F}_{12} + \vec{F}_{21} = 0$$

Ex -> Walking  
Swimming  
Requiling of gun when bullet is fired.  
\* Propulsion of Rocket

- NOTE ->
- \* Action Reaction is applied on two diff object.
  - \* In a universe single force is not produce it is possible in pair.
  - \* There is no time lack b/w action & Reaction so be can't say than action is produce by Reaction or vice-versa.
  - \* Action Reaction law is applicable on all natural force. (gravitational force, EMW, Nuclear force, weak force)
  - \* Newton 3rd law is applicable in linear momentum conservation.
  - \* From Newton 2nd law we explain Newton 1st & 3rd law.

# # Rocket propulsion [ex of Newton's 3rd Law]



$\frac{dm}{dt}$  = Rate of change in mass / Rate of mass ejection.

$v$  = velo. of gas.

$$|F_{ex} = v \frac{dm}{dt}|$$

$$v \frac{dm}{dt} - mg = ma \quad \text{Acceleration of Rocket.}$$

#  $a = 0$  (Move w const velo)

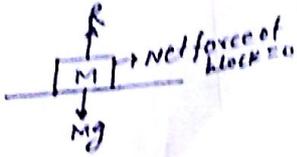
$$v \frac{dm}{dt} - mg = m(0)$$

$$* \left[ v \frac{dm}{dt} = mg \right]$$

## # Normal Reaction

|a|  $\rightarrow$  Rest

$$R = Mg$$

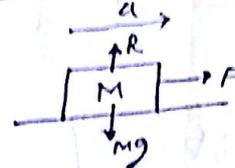


|b|  $\rightarrow$  Horizontal force

ii  $\rightarrow$

$$R = Mg$$

$$a = \frac{F}{M}$$



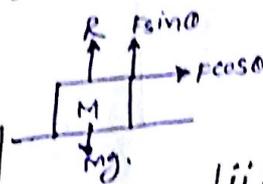
|c|  $\rightarrow$  Force app. at an angle  $\theta$  from Horizontal.

ii  $\rightarrow$

$$F \sin \theta < Mg$$

$$a = \frac{F_{net}}{m_{net}} = \frac{F \cos \theta}{M}$$

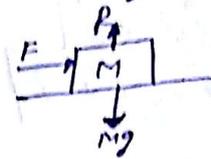
$$R = Mg - F \sin \theta < Mg$$



iii  $\rightarrow$

$$R = Mg$$

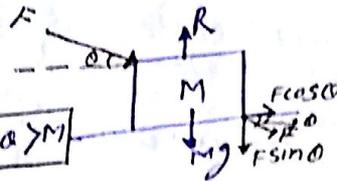
$$a = \frac{F}{M}$$



iii  $\rightarrow$

$$a = \frac{F \cos \theta}{M}$$

$$R = Mg + F \sin \theta > Mg$$

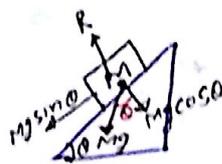


|d|  $\rightarrow$  Incline surface.

ii  $\rightarrow$   $F_x = 0$

$$R = Mg \cos \theta$$

$$a = g \sin \theta$$



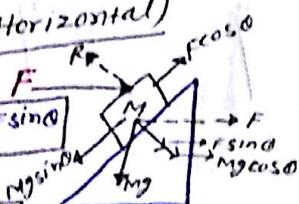
iii  $\rightarrow$   $F_x \neq 0$  (Horizontal)

$$R = Mg \cos \theta + F \sin \theta$$

$$Mg \sin \theta > F \cos \theta$$

$$a = \frac{F_{net}}{m_{net}} = \frac{F_x - F_y}{M_{net}}$$

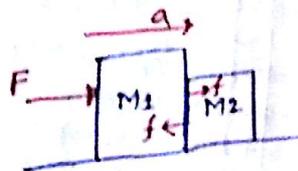
$$a = \frac{Mg \sin \theta - F \cos \theta}{M}$$



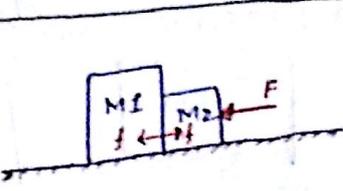
# When object place in a contact in a Smooth Horizontal surface.

|a|  $\rightarrow$  Two object

$$a = \frac{F}{M_1 + M_2}$$



# contact force(s)  $f = M_2 a = \frac{M_2 F}{M_1 + M_2}$

$$a = \frac{F}{M_1 + M_2} \quad f = \frac{M_1 F}{M_1 + M_2}$$


1b) → Three object

$$a = \frac{F_{net}}{m_{net}} = \frac{F}{M_1 + M_2 + M_3}$$



$$* f_1 = (M_2 + M_3)a = \frac{(M_2 + M_3)F}{M_1 + M_2 + M_3}$$

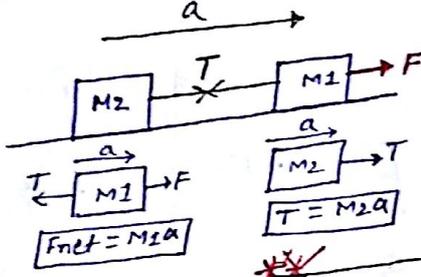
$$* f_2 = M_3 a = \frac{M_3 F}{M_1 + M_2 + M_3}$$

# Mass-string system

1) →

$$a = \frac{F}{M_1 + M_2}$$

$$T = M_2 a = \frac{M_2 F}{M_1 + M_2}$$



$$* a = \frac{F_{net}}{\Sigma M} = \frac{F_s - F_a}{\Sigma M}$$

$$T = \frac{F_f M_b + F_b M_f}{\Sigma M}$$

~~Supporting force - opposing force~~  
~~Total mass~~  
~~Forward force x backward mass + backward force x forward mass~~  
~~Total mass~~

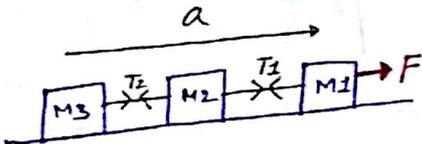
2) →

$$a = \frac{F_{net}}{\Sigma M} = \frac{F}{M_1 + M_2 + M_3}$$

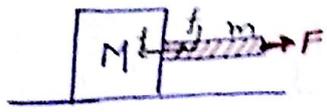
$$T_1 = \frac{F(M_2 + M_3) + 0(M_1)}{M_1 + M_2 + M_3}$$

$$= \frac{(M_2 + M_3)F}{M_1 + M_2 + M_3}$$

$$T_2 = \frac{F(M_3) + 0(M_2 + M_1)}{M_1 + M_2 + M_3} = \frac{M_3 F}{M_1 + M_2 + M_3}$$



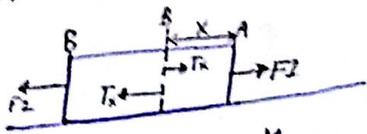
# Block of mass 'M' connect with string of mass 'm'. Force 'F' is applied at free end of string then force applied on mass 'M'.



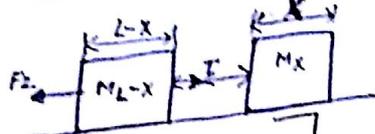
$$a = \frac{F}{M+m}$$

$$f = Ma = \frac{MF}{M+m}$$

# Rod of length 'L' placed on horizontal surface. Force 'F<sub>1</sub>' & 'F<sub>2</sub>' force is applied on free end of Rod in opposite direction. Then tension in a Rod at distance 'X' from F<sub>2</sub> force.



$$a = \frac{F_{net}}{\Sigma M} = \frac{F_1 - F_2}{M}$$



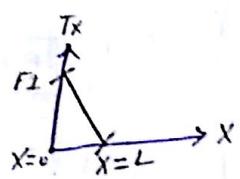
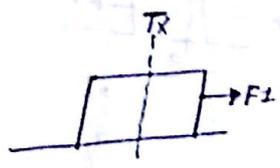
$$T = \frac{F_1 m_b + F_2 m_f}{m_b + m_f}$$

$$T_x = F_1 \left(1 - \frac{X}{L}\right) + F_2 \left(\frac{X}{L}\right)$$

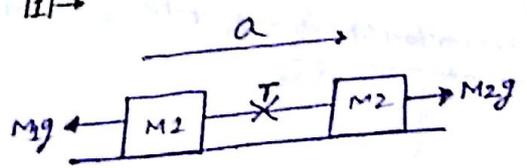
$$\begin{aligned} L &= M \\ L-X &= \frac{M}{L}(L-X) = M-L-X \\ X &= \frac{M}{L}X = Mx \end{aligned}$$

# F<sub>2</sub> = 0

$$T_x = F_1 \left(1 - \frac{X}{L}\right)$$



# Mass pulley system

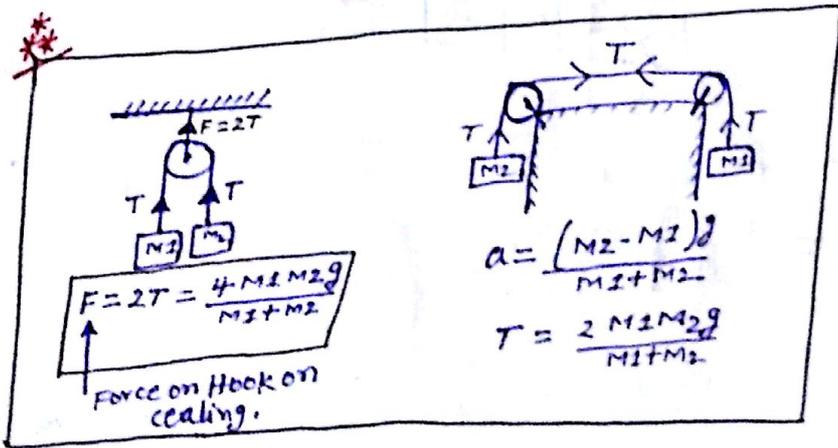


$$* a = \frac{F_{net}}{\Sigma M} = \frac{F_s - F_a}{\Sigma M} = \frac{M_2 g - M_1 g}{M_1 + M_2}$$

$$a = \frac{(M_2 - M_1)g}{M_1 + M_2}$$

$$* T = \frac{F_1 m_b + F_2 m_f}{\Sigma M} = \frac{(M_2 g)(M_1) + (M_1 g)(M_2)}{M_1 + M_2}$$

$$T = \frac{2 M_1 M_2 g}{M_1 + M_2}$$



$$a = \frac{(M_2 - M_1)g}{M_1 + M_2}$$

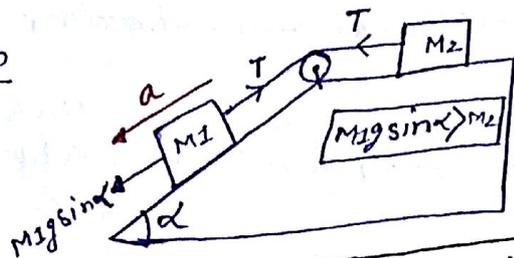
$$T = \frac{2 M_1 M_2 g}{M_1 + M_2}$$

NOTE  
Tension are internal force.  
 $\Sigma \vec{T} \cdot \vec{v} = 0$   
 $P = \vec{F} \cdot \vec{v}$   
\* Internal force never develop power

12) →

$$a = \frac{F_{net}}{\Sigma F} = \frac{M_1 g \sin \alpha - 0}{M_1 + M_2}$$

$$a = \frac{M_1 g \sin \alpha}{M_1 + M_2}$$

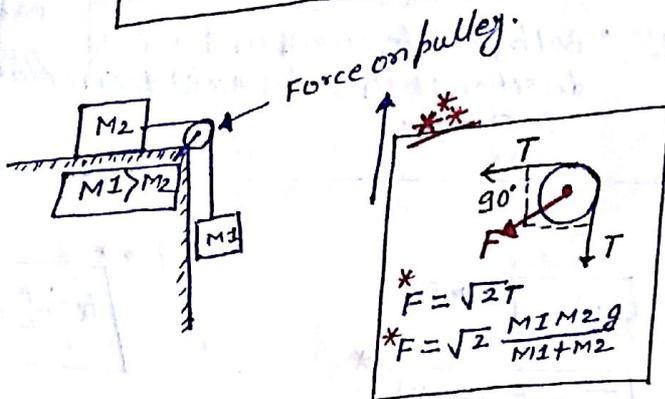


$$T = \frac{M_1 g \sin \alpha (M_2) + 0 (M_1)}{M_1 + M_2} = \frac{M_1 M_2 g \sin \alpha}{M_1 + M_2}$$

13) →

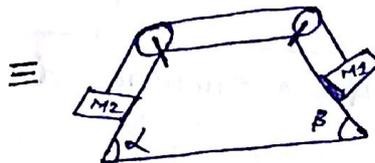
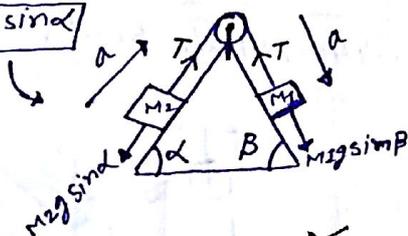
$$a = \frac{M_1 g}{M_1 + M_2}$$

$$T = \frac{M_1 M_2 g}{M_1 + M_2}$$



14) →

$$M_1 g \sin \beta > M_2 g \sin \alpha$$



$$* a = \frac{F_{net}}{\Sigma M} = \frac{M_1 g \sin \beta - M_2 g \sin \alpha}{M_1 + M_2}$$

$$T = \frac{(M_1 g \sin \beta)(M_2) + (M_2 g \sin \alpha)(M_1)}{M_1 + M_2}$$

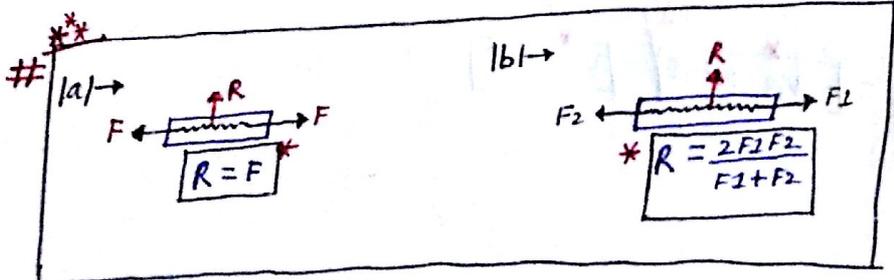
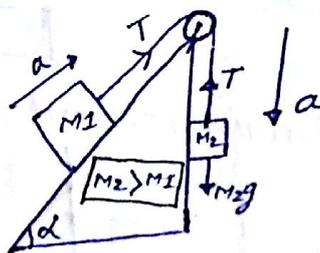
$$* T = \frac{M_1 M_2 g (\sin \alpha + \sin \beta)}{M_1 + M_2}$$

15) →

$$a = \frac{F_{net}}{\Sigma M} = \frac{M_2 g - M_1 g \sin \alpha}{M_1 + M_2}$$

$$T = \frac{M_2 g (M_1) + (M_1 g \sin \alpha)(M_2)}{M_1 + M_2}$$

$$T = \frac{M_1 M_2 g (1 + \sin \alpha)}{M_1 + M_2}$$



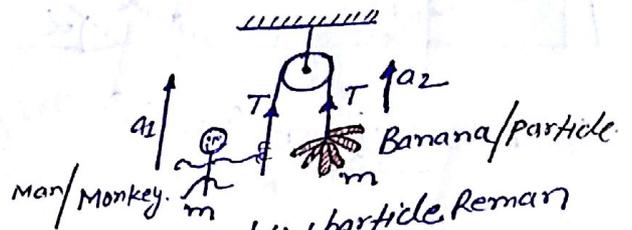
**NOTE** → \* If person move in a downward direction with const acceleration than tension in string is less than from weight of person.  
 \* When a move in a upward direction with const acceleration than tension in string more than weight of person.

**\*\* #** Mass of person & Banana is 'm' & it is arranged in pulley as shown. If person move upward with const acceleration than distance b/w person & Banana.

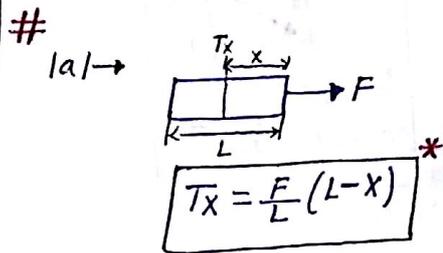
$$T = mg = ma_1 \rightarrow \text{I}$$

$$T - mg = ma_2 \rightarrow \text{II}$$

$$a_1 = a_2$$

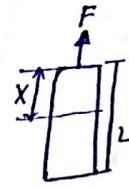


**NOTE** → Both particle moves in same direction with same acceleration than relative distance b/w particle remain unchange.



|b| → \*

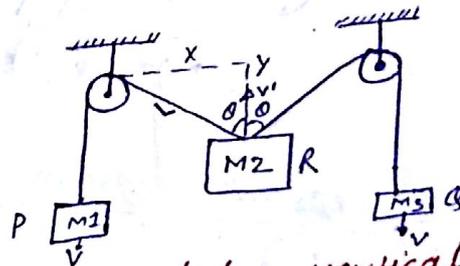
$$T_x = \frac{F}{L}(L-x)$$



**#** Mass 'p' & 'q' move downward direction with speed 'v' than speed of mass 'r'.

$$v' = v \left( \frac{L}{y} \right)$$

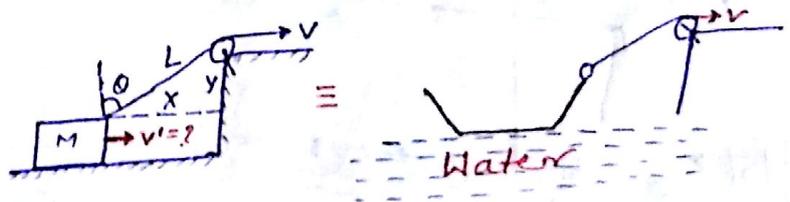
$$v' = \frac{v}{\frac{y}{L}} = \frac{v}{\cos \theta}$$



**#** velocity of mass 'm' on horizontal plane when angle from vertical is 'theta'.

$$L^2 = x^2 + y^2$$

$$v' = \frac{v}{\sin \theta}$$



**AMU #** velocity of end 'A' in given instant.

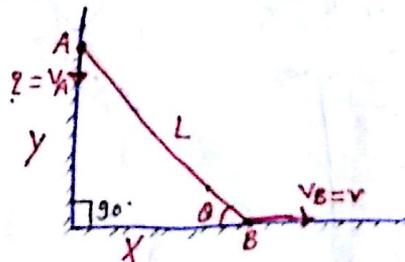
$$L^2 = x^2 + y^2$$

$$2L \left( \frac{dL}{dt} \right) = 2x \left( \frac{dx}{dt} \right) + 2y \left( \frac{dy}{dt} \right)$$

$$2L(0) = 2x(v_B) + 2y(v_A)$$

$$v_A = -v_B \left( \frac{x}{y} \right)$$

$$v_A = -\frac{v_B}{\frac{y}{x}} = \frac{-v_B \cos \theta}{\sin \theta} = -v_B \cot \theta = v_A \cos \theta$$



# # Frame of Reference

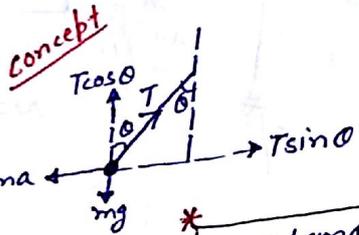
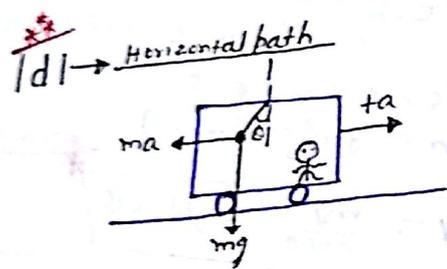
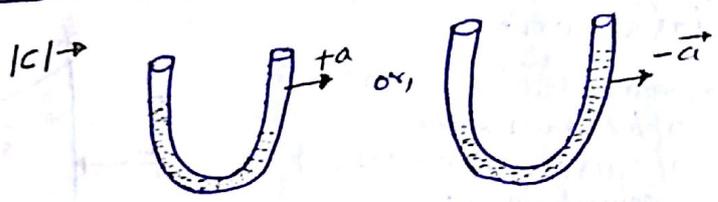
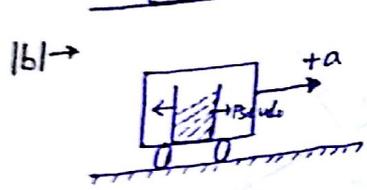
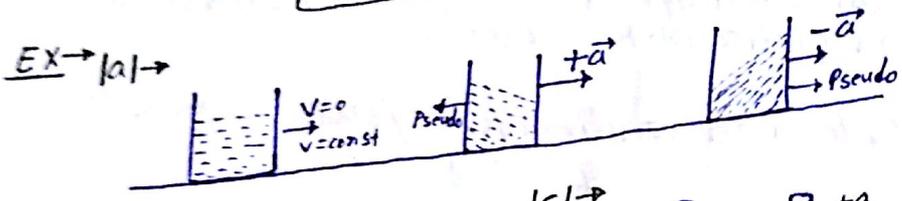
**Ia) Inertial frame of Reference** → If system or frame is at rest or move with const velocity.  
 \* Law of Inertia applicable on Inertial frame of Reference.  
 \* Earth, around consider as Inertial frame of Reference.

**Ib) Non-inertial frame of Reference** → If system or frame is accelerated (speedup or slowdown).  
 \* Law of Inertia is not applicable.  
 \* In a non-inertial frame, Pseudoforce is applicable on particle.

## # Pseudoforce

Appear/ent in only non-inertial frame of Reference. With the help of Pseudoforce we convert Non-inertial into Inertial frame & direction of Pseudoforce is opposite to the direction of Acceleration.

$$\text{Pseudoforce} = F = -ma$$



$$T \cos \theta = ma \quad \text{--- (I)}$$

$$T \sin \theta = mg \quad \text{--- (II)}$$

ii)  $\frac{T \sin \theta}{T \cos \theta} = \frac{mg}{ma} = \tan \theta \Rightarrow \frac{a}{g} \Rightarrow a = g \tan \theta$

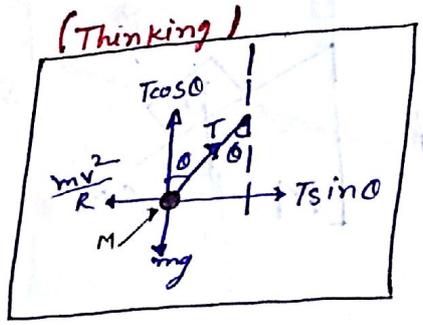
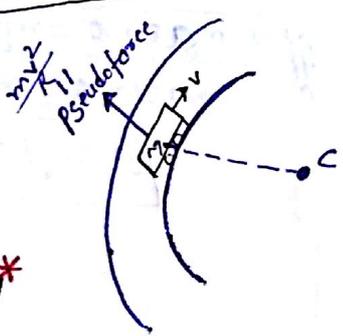
iii)  $(T \sin \theta)^2 + (T \cos \theta)^2 = (mg)^2 + (ma)^2$   
 $T = \sqrt{(mg)^2 + (ma)^2}$

**\* |e| → circular path**

$$T \cos \theta = mg \quad \text{--- (I)}$$

$$T \sin \theta = \frac{mv^2}{R} \quad \text{--- (II)}$$

$\tan \theta = \frac{v^2}{Rg} \Rightarrow \theta = \tan^{-1} \left( \frac{v^2}{Rg} \right)$   
 $T = \sqrt{(mg)^2 + \left( \frac{mv^2}{R} \right)^2}$



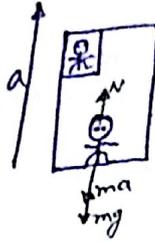
**|f| → Motion of Lift**

|a| → Moving upward

$$N_{up} = mg + ma$$

$$W_{eff} = mg + ma > W$$

$$g_{eff} = \frac{W_{eff}}{m} = g + a$$

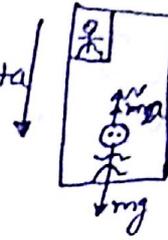


**|b| → Moving downward**

$$N_{down} = mg - ma$$

$$W_{eff} = mg - ma < W$$

$$g_{eff} = g - a$$



|c| → Moving with const velocity

$$a = 0 \Rightarrow \text{Pseudoforce} = 0$$

$$W_{eff} = mg = W$$

$$g_{eff} = g$$

|d| → In downward direction

ii) → Free falling cond. ( $a = g$ )

$$N = 0 = W_{eff}$$

$$g_{eff} = 0$$

iii) →  $a > g$

$$N = \ominus ve = W_{eff}$$



**BHU NOTE**

→ \* Effective Weight of person in a lift is greater than from Actual Weight when lift move with upward with const. Acc. & downward with const. Retardation.

**# Body of mass 'm' placed on a inclined plane/Wedge of mass 'M' as shown.**

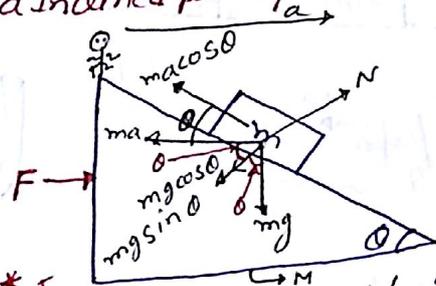
ii) → Magnitude of Horizontal force applied on Wedge 'M' so block of mass 'm' remain in equilibrium.

$$m \cos \theta = mg \sin \theta$$

$$a = g \tan \theta$$

$$F = (M+m)a$$

$$F = (M+m)g \tan \theta$$



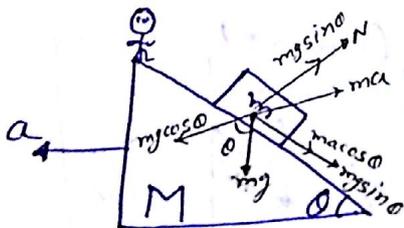
\* AIPMT iii) → Force applied by 'm' on the wedge.

$$N = m \sin \theta + mg \cos \theta$$

$$= mg \left( \frac{\sin^2 \theta}{\cos \theta} + \cos \theta \right)$$

$$N = \frac{mg}{\cos \theta} = mg \sec \theta$$

**# Acceleration of Wedge 'M' If block of mass 'm' fall freely.**



$$N + mg \sin \theta = mg \cos \theta$$

$$m \sin \theta = mg \cos \theta$$

$$a = g \cot \theta$$

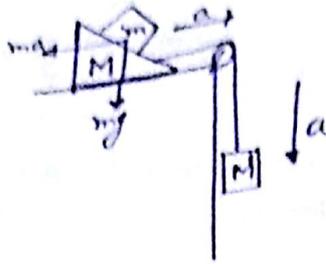
\* NOTE → \*  $a > g \tan \theta \Rightarrow$  block 'm' move upward.  
\*  $a < g \tan \theta \Rightarrow$  block 'm' move downward.

# Value of  $M'$ . If 'm' is in a cart with mass  $M$ .

$a = g \tan \theta$

$a = \frac{m'g}{M+m+M'} = g \tan \theta$

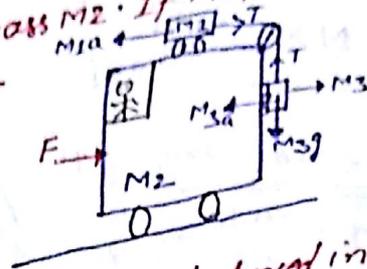
$M' = \frac{(M+m) \tan \theta}{1 - \tan \theta}$



# Magnitude of Horizontal force applied on mass  $M_2$ . If  $M_1$  &  $M_3$  are in eqm.

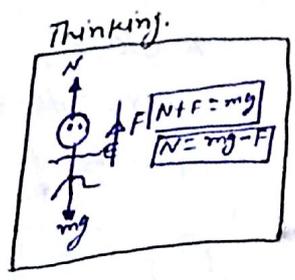
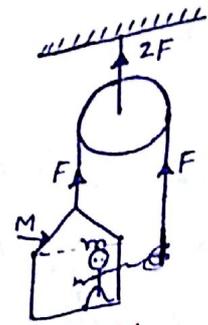
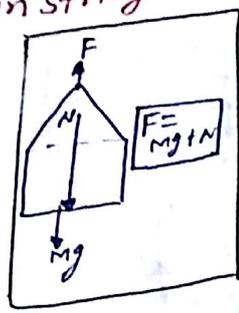
$T = M_3 g$   
 $T = M_1 a$   
 $M_1 a = M_3 g$   
 $a = \left(\frac{M_3}{M_1}\right) g$

$F = (M_1 + M_2 + M_3) \left(\frac{M_3}{M_1}\right) g$



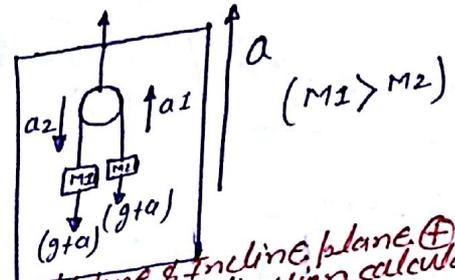
# Force Applied by person in string if system remain balanced in air.

$F = Mg + N$   
 $F = \frac{(M+m)g}{2}$



# Tension in a string which is connected with mass & lift moving upward with acceleration 'a'.

$T = \frac{2M_1 M_2 (g+a)}{M_1 + M_2}$



# If particle drop along the surface inclined plane & incline plane is in a lift which is moving with const. acceleration in upward direction calculate time by particle to reach at bottom.

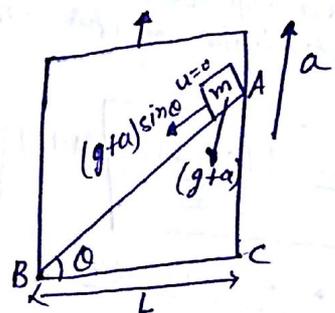
$u = 0, a = (g+a) \sin \theta$

$\cos \theta = \frac{BC}{AB} = \frac{AB}{L} = \frac{L}{\cos \theta}$

$S = ut + \frac{1}{2} at^2$

$\frac{L}{\cos \theta} = (0) + \frac{1}{2} [(g+a) \sin \theta]^2 t^2$

$t = \sqrt{\frac{2L}{(g+a) \sin \theta \cos \theta}}$



concept  
 When jump then weight on head become zero

# % change in weight when lift is moving upward & downward with acceleration 'a'

$$\frac{\Delta W}{W_{actual}} = \frac{W_{up} - W_{actual}}{W_{actual}} = \frac{a}{g} \times 100$$

$$W_{actual} = mg$$

$$W_{up} = m(g+a)$$

Tibber 2016  
(NOT IN AIPMT) But other PMT  
Simple Machine

11) → Mechanical Advantage (M.A)

$$M.A = \frac{Load(L)}{Effort(E)}$$

12) → Velocity Ratio (V.R)

$$V.R = \frac{V_E}{V_L} = \frac{dE/dt}{dL/dt} = \frac{dE}{dL}$$

13) → Mechanical Efficiency (η)

$$\eta = \frac{M.A}{V.R} = \frac{L/E}{dE/dL} = \frac{LdL}{EdE} = \frac{\text{Work done by load}}{\text{Work done by the effort}}$$

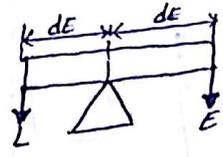
14) → Lever System

# Class I

$$dL \cdot XL = dE \cdot XE$$

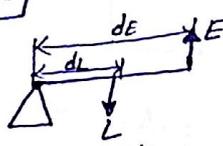
$$M.A = \frac{L}{E} = \frac{dE}{dL}$$

→ may be M.A > 1  
→ may be M.A < 1  
→ may be M.A = 1



#

$$M.A = \frac{L}{E} = \frac{dE}{dL} > 1$$



#

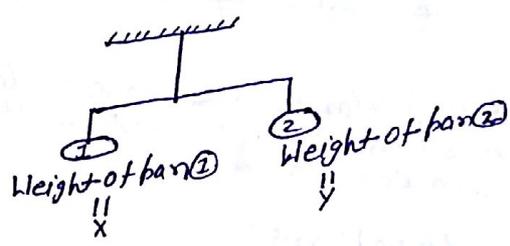
$$M.A = \frac{L}{E} = \frac{dE}{dL} < 1$$



15) → False Balance

Case I → Length same

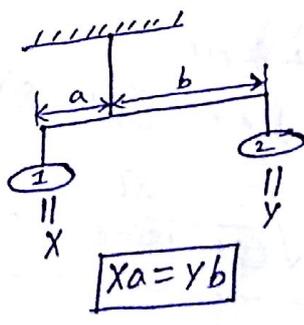
- \* W = Actual wt of object
- \* W1 = weight of obj. when placed on pan ①
- \* W2 = " " " " " " " " " " ②



$$* W = \frac{W1 + W2}{2} \quad (A.M)$$

Case II → Length unequal

$$* W = \sqrt{W1 W2} \quad (G.M)$$



# If  $f_1 = f_2 = f$

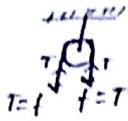
$$T_x = f\left(1 - \frac{x}{l}\right) + f\left(\frac{x}{l}\right)$$

$$T_x \propto f \propto x^0$$


$$T_1 = T_2 = T_3 = f$$

# Mass pulley system

Fixed pulley



$$T_{net} = Rf - Rf = 0$$

pulley rotate



$$T_1 > T_2$$

$$T_{net} = RT_1 - RT_2 \neq 0$$